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Review

# Mechanism and kinetics of thermal decomposition of carbonates

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#### Abstract

A physical approach to the interpretation of the mechanisms and kinetics of thermal decomposition of solids has been applied to the investigation of decomposition mechanisms of Ag, Cd, Zn, Mg, CaMg, Ca, Sr and Ba carbonates. The method consists in comparing experimental literature data on the kinetic parameters with their theoretical values calculated on the basis of the physical approach. Two parameters were used: the *E* parameter and the initial temperature of decomposition,  $T_{in}$ , defined as the temperature of decomposition which corresponds to the fixed partial pressure,  $P_{in}$ , of CO<sub>2</sub> evolved. The results of examination of the available data supported the general mechanism of decomposition which includes as a primary stage the congruent dissociative evaporation of reactants. For all the carbonates, except of BaCO<sub>3</sub>, the transfer to the reactant one-half of the energy released in the course of the condensation of low-volatility product has been taken into account in the calculations. The effect of self-cooling on the results of experimental determination of both parameters has been examined, and several important conclusions has been deduced. In particular, in the decomposition of CaCO<sub>3</sub> in the presence of CO<sub>2</sub> ( $10^{-6}$ –  $10^{-4}$  bar), the self-cooling effect is responsible for the lack of expected hyperbolic dependence of decomposition rate on CO<sub>2</sub> pressure and the appearance of the Topley–Smith effect. Several quantitative criteria of the validity of measured *E* values has been proposed. On this basis, the values of *E* parameters reported in the literature were critically analysed. © 2002 Elsevier Science B.V. All rights reserved.

Keywords: Physical approach; Decomposition; Mechanisms; Carbonates; Self-cooling

### 1. Introduction

The mechanism and kinetics of thermal decomposition of carbonates (in particular, calcium carbonate) have been dealt with a large number of studies summed up partially in a review [1] and monographs [2,3]. Nevertheless, there are still no quantitatively substantiated models of carbonate decomposition. No explanation has been also given for some unusual features in their decomposition exemplified below.

- 1. Anomalous scatter among the kinetic parameters of the Arrhenius equation (E and A) available in the literature for decomposition of CaCO<sub>3</sub>, particularly measured by non-isothermal methods in the presence of CO<sub>2</sub> [4,5].
- 2. A  $10^4-10^5$ -fold difference observed in the decomposition of CaCO<sub>3</sub>, CaMg(CO<sub>3</sub>)<sub>2</sub> and BaCO<sub>3</sub> in the Knudsen mode (the effusion cell) and under Langmuir conditions (from an open surface), or, in other words, low vaporization coefficients,  $\alpha_v$ , for these compounds in vacuum [6,7]. This is in contradiction with a widespread statement of their partly reversible decompositions.

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3. Discrepancy in the dependence of decomposition rates of CaCO<sub>3</sub> on CO<sub>2</sub> background pressures observed by different authors. In contrast to the observation of hyperbolic rate law ( $\propto 1/P_{CO_2}$ ) in [8–10], Darroudl and Searcy [11] observed close to linear decrease of the decomposition rate with the background pressure of CO<sub>2</sub>.

The objective of this work is in presenting an interpretation for the above and related aspects by applying a physical approach to explanation of the thermal decomposition mechanism, which is based on a scheme involving dissociative evaporation of the reactant with simultaneous condensation of the low-volatile product. This approach advanced by Hertz and Langmuir and developed by the author has been successfully employed earlier in the interpretation of the mechanism and kinetics of thermal decomposition of metal oxides [12–14], nitrates [15–17], azides [18], Li<sub>2</sub>SO<sub>4</sub>:H<sub>2</sub>O [19], Mg(OH)<sub>2</sub> [20], GaN [21], oxalates [22] and of a number of other inorganic compounds [23].

Our earlier attempt [24] to interpret the decomposition mechanism of alkaline-earth carbonates as a result of the carbonate interaction with residual water vapor in the reactor was not successful. The good agreement between calculated and experimental values of the *E* parameter was accompanied by  $10^3-10^4$  differences of the calculated rates of decompositions from experimental data. Two important factors have not been taken into account in that work [24]: the effect of self-cooling on measured values of the *E* parameter and the partial transfer of the energy released in the condensation of low-volatility product (MO) to the reactant.

#### 2. Theoretical model

The scheme employed in the theoretical calculation of the main kinetic parameters of the decomposition process (the flux of the gaseous product J, the rate constant k, the product partial pressure P and the parameters of the Arrhenius equation, E and A) has been described in a number of our recent publications [19–22], especially, in a review [23]. Therefore, we are going to present below only some final relations necessary for the calculations in this work.

### 2.1. Decomposition in vacuum

In the case of a compound S decomposed into gaseous products A and B, i.e.

$$S(s) \rightarrow aA(g) + bB(g)$$
 (1)

the flux of product A can be expressed through the partial pressure  $P_A$  (in atm) of this product corresponding to the hypothetical equilibrium of reaction (1) in the form

$$I = \frac{\gamma N_{\rm A} P_{\rm A}}{\left(2\pi M_{\rm A} RT\right)^{1/2}}\tag{2}$$

where  $N_A$  is the Avogadro number and  $M_A$  the molar mass of product A. Here  $\gamma = 101\,325\,\text{Pa}\,\text{atm}^{-1}$  is the conversion factor from atmospheres to pascals. This relationship derived as shown here by Langmuir [25] is usually called the Hertz–Langmuir equation.

In the case of evaporation of spherical particles, the rate constant is as follows [24]:

$$k = \frac{JM_{\rm r}}{N_{\rm A}\rho r_0} \tag{3}$$

where  $\rho$  and  $M_r$  are the density and molar mass of the reactant.

2.2. Equilibrium pressure of product for dissociative evaporation

The partial pressure,  $P_A$ , of product A can be calculated from the equilibrium constant,  $K_P$ , for reaction (1). In the absence of reaction products in the reactor atmosphere, the situation corresponding to the *equimolar* evaporation mode, the partial pressure  $P_A$  can be expressed [26] as

$$P_{\rm A}^{\rm e} = a \left(\frac{K_{\rm P}}{F}\right)^{1/\nu} \left(\frac{M_{\rm A}}{M_{\rm B}}\right)^{b/2\nu} = \frac{a}{F^{1/\nu}} \left(\frac{M_{\rm A}}{M_{\rm B}}\right)^{b/2\nu} \exp \frac{\Delta S_{\rm T}^{\rm o}}{\nu R} \exp \left(-\frac{\Delta_{\rm r} H_{\rm T}^{\rm o}}{\nu RT}\right)$$
(4)

where

$$F \equiv a^a \times b^b \tag{5}$$

$$v = a + b \tag{6}$$

and

$$K_{\rm P} = P_{\rm A}^a \times P_{\rm B}^b \tag{7}$$

Here  $\Delta_r H_T^o$  and  $\Delta S_T^o$  are, respectively, the changes of the enthalpy and entropy in reaction (1).

If the partial pressure  $P'_{\rm B}$  of one of the gaseous components (B) greatly exceeds the equivalent pressure  $P_{\rm B}$  of the same component released in the decomposition and if, in addition to that, the magnitude of  $P'_{\rm B}$ remains constant in the process of decomposition, we call such an evaporation mode *isobaric*. In this case

$$P_{\rm A}^{\rm i} = \frac{K_{\rm P}^{1/a}}{\left(P_{\rm B}'\right)^{b/a}} = \frac{1}{\left(P_{\rm B}'\right)^{b/a}} \exp\frac{\Delta S_{\rm T}^{\rm o}}{aR} \exp\left(-\frac{\Delta_{\rm r}H_{\rm T}^{\rm o}}{aRT}\right)$$
(8)

In order to take into account the partial transfer of the energy released in the condensation of low-volatility product A to the reactant, we introduce into the calculations of the enthalpy of decomposition reaction (1) an additional term,  $\tau a \Delta_c H_T^o$  (A), where the coefficient  $\tau$  corresponds to the fraction of the condensation energy transferred to the reactant. Thus, we can write

$$\Delta_{\rm r} H_{\rm T}^{\rm o} = a \,\Delta_{\rm f} H_{\rm T}^{\rm o}({\rm A}) + b \,\Delta_{\rm f} H_{\rm T}^{\rm o}({\rm B}) - \Delta_{\rm f} H_{\rm T}^{\rm o}({\rm S}) + \tau a \,\Delta_{\rm c} H_{\rm T}^{\rm o}({\rm A})$$
(9)

The most plausible of all conceivable mechanisms for the energy transfer appears to be thermal accommodation [27] or, in other words, direct transfer of the energy at the reaction interface by collisions of the low-volatility molecules with the reactant and the product surface. For equal temperatures of the solid phases, one may expect equipartition of energy between the two phases, i.e.,  $\tau = 0.5$ . For the majority of substances investigated up to now, the condition  $\tau = 0.5$  is found to be valid.

#### 2.3. Theoretical calculation of Arrhenius parameters

Eqs. (2)–(9) can be used for the calculation of the main parameters determining the kinetics of sublimation/decomposition processes: the evaporation rate J, the initial temperature  $T_{in}$ , and two traditional Arrhenius parameters, entering the Arrhenius equation:

$$k = A \exp\left(-\frac{E}{RT}\right) \tag{10}$$

As can be seen from Eqs. (4) and (8), the *E* parameter for reaction (1) should be different for the

equimolar and isobaric modes of decomposition, i.e.,

$$E^{\rm e} = \frac{\Delta_{\rm r} H_{\rm T}^{\rm o}}{v} = \frac{\Delta_{\rm r} H_{\rm T}^{\rm o}}{a+b} \tag{11}$$

for the equimolar mode and

$$E^{i} = \frac{\Delta_{\rm r} H^{\rm o}_{\rm T}}{v - b} = \frac{\Delta_{\rm r} H^{\rm o}_{\rm T}}{a} \tag{12}$$

for the isobaric mode. In both cases, the *E* parameter corresponds to the *specific enthalpy*, i.e., the enthalpy of the decomposition reaction reduced to 1 mol of primary products without including components of that present in excess.

By combining Eqs. (4), (8) and (10) with Eqs. (2) and (3), it is easy to obtain the relationships for the calculation of the *A* parameter. For example, in the case of decomposition of spherical particles in vacuum (the equimolar mode) in accordance with process (1), by combination of Eqs. (2)–(4) and (10), we obtain

$$A^{e} = \frac{\gamma M_{r}}{\rho r_{0} (2\pi M_{A}RT)^{1/2}} \frac{a}{F^{1/\nu}} \left(\frac{M_{A}}{M_{B}}\right)^{b/2\nu} \exp \frac{\Delta S_{T}^{o}}{\nu R}$$
$$= \frac{\gamma M_{r}}{\rho r_{0} (2\pi \overline{M}RT)^{1/2}} \frac{a}{F^{1/\nu}} \exp \frac{\Delta S_{T}^{o}}{\nu R}$$
(13)

where  $\overline{M}$  is the geometrical mean between  $M_A$  and  $M_B$ , i.e.,  $\overline{M} = (M_A \times M_B)^{1/2}$ . In the case of decomposition of spherical particles in the presence of excess of the gaseous component B (the isobaric mode), by combination of Eqs. (2), (3), (8) and (10), we obtain

$$A^{i} = \frac{\gamma M_{\rm r}}{\rho r_0 (2\pi M_{\rm A} R T)^{1/2}} \frac{1}{(P_{\rm B}')^{b/a}} \exp \frac{\Delta S_{\rm T}^{\rm o}}{aR}$$
(14)

As can be seen from theoretical modelling of the evaporation processes above, by combination of the different equations it is possible to obtain the final formulae for the calculation of the *A* parameter under different experimental conditions. These equations take into account many parameters describing the properties of solid reactant and primary products (thermodynamic functions, molar mass, density), the sample distribution (a monolayer or spherical particles of known radius), experimental conditions (temperature), and the evaporation modes (equimolar or isobaric) including, in the last case, the value of the excess pressure of the gaseous product. As a result, the *A* values may vary within very wide limits. For example, for a simple reaction of the type  $S(s) \rightarrow A(g)$ 

+bB(g), the ratio of the *A* parameters for the isobaric and equimolar modes of evaporation equals

$$\frac{A^{i}}{A^{e}} \simeq \frac{1}{\left(P'_{\rm B}\right)^{b}} \exp \frac{b \,\Delta S^{\rm o}_{\rm T}}{(b+1)R} \tag{15}$$

Substituting into Eq. (15) rather typical values for these parameters:  $\Delta S_{\rm T}^{\rm o}/(b+1) = 150 \,\mathrm{J}\,\mathrm{mol}^{-1}\,\mathrm{K}^{-1}$ (see below) and  $P_{\rm B}' = 10^{-5}$  bar, we obtain  $A^{\rm i}/A^{\rm e} \cong$  $3 \times 10^{6}$  for  $b = 0.5, A^{\rm i}/A^{\rm e} \cong 7 \times 10^{12}$  for b = 1 and  $A^{\rm i}/A^{\rm e} \cong 2 \times 10^{19}$  for b = 1.5. Therefore, the isobaric mode of decomposition, compared to the equimolar mode, results in much higher values of the *A* parameter.

As shown above, this approach allows calculation of both parameters of the Arrhenius equation (E and A). This means that the absolute rates of the dissociative evaporation can be theoretically calculated. Attempts to solve this problem in the framework of the traditional (chemical) approach using for this purpose the ideas of transition-state theory (with another name 'theory of absolute reaction rates') were unsuccessful. These attempts (e.g. [28]) have not progressed beyond very approximate estimations of the pre-exponential or frequency factor (in the range  $10^{14}$ - $10^{16}$  s<sup>-1</sup>) though, actually, the A values are far beyond these limits and in many cases becomes larger than  $10^{20} \text{ s}^{-1}$  or lower than  $10^{10} \text{ s}^{-1}$  [29]. The value of the activation energy in these calculations was usually kept in the shadows.

# 2.4. Theoretical calculation of initial temperature of decomposition in vacuum

Taking logarithms and solving Eq. (4) for the temperature contained in the enthalpy factor, we obtain the following relationship for the calculation of the initial temperature of decomposition:

$$T_{\rm in} = \frac{\Delta_{\rm r} H_{\rm T}^{\rm o}}{\Delta S_{\rm T}^{\rm o} + \nu R [\ln q - \ln F / \nu + (b/2\nu) \ln(M_A/M_B) - \ln P_{\rm in}]}$$
(16)

where  $P_{in}$  is the partial pressure of product A corresponding to the initial temperature.

Neglecting the first three insignificant items in the square brackets of Eq. (16) and taking into account Eq. (11), we come to the important relationship

$$\frac{T_{\rm in}}{E} \simeq \frac{1}{\Delta S_{\rm T}^{\rm o}/v - R \ln P_{\rm in}} \tag{17}$$

Taking into account that for sublimation or dissociative evaporation of one mole of solid (metal or compound) at the temperature of the initial decomposition, the average value of  $\Delta S_{\rm T}^{\rm o}/\nu = 150 \pm 30 \,\mathrm{J}\,\mathrm{mol}^{-1}\,\mathrm{K}^{-1}$ [12–16,18–22,26] and that the initial temperature corresponds approximately to  $P_{\rm in} = 10^{-7}$  bar [14], we obtain  $T_{\rm in}/E \cong 3.5 \pm 0.4 \,\mathrm{K}\,\mathrm{mol}\,\mathrm{kJ}^{-1}$ . The proportional dependence of the initial/appearance temperature on the *E* parameter was pointed out on purely empirical grounds in electrothermal atomic absorption spectrometry in the 1970s [30–32]. However, only in the framework of the physical approach has it received a rigorous theoretical explanation.

The relationship (17) can be considered as a generalization of the well-known Trouton's rule relating the boiling temperature  $(T_b)$  and the molar enthalpy of vaporization  $(\Delta H_T^o)$  of liquids (see, e.g. [33]). At the boiling point when P = 1 bar, the average value of  $\Delta S_T^o / \nu$  (for a majority of liquids) is about  $86 \pm 20 \,\mathrm{J}\,\mathrm{mol}^{-1}\,\mathrm{K}^{-1}$  [33] and, as a result,  $T_b / \Delta H_T^o$  ranges from 9.4 to 15.2 K mol kJ<sup>-1</sup>.

### 3. Results and discussion

#### 3.1. Preliminary comments

The method to be employed below consists in comparing experimental data on the kinetic parameters with their theoretical values calculated on the basis of the physical approach outlined above. Two parameters will be used: the *E* parameter and the initial temperature of decomposition,  $T_{in}$ , defined as the temperature of decomposition which corresponds to the fixed partial pressure,  $P_{in}$ , of CO<sub>2</sub> evolved. These parameters completely describe the kinetics of steady-state decomposition (in equimolar mode) at any temperature. The choice of metal carbonates for analysis in this study was defined by the availability in the literature of proper experimental data on the decomposition kinetics and reliable thermodynamic functions for reactants and products for the corresponding theoretical calculations. On this basis, carbonates of Ag, Cd, Zn, Mg, CaMg, Ca, Sr and Ba have been chosen. Table 1 presents the results of a correlation between experimental [6,7,11,34–48] and theoretical data. We will give below some comments on the origin of these data.

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Carbonate	$T_{\rm in}$ (K)			$\alpha_{\rm v}$		$E^{\rm e}$ (kJ mol <sup>-1</sup> )		$E^{i}$ (kJ mol <sup>-1</sup> )		$P'_{\rm CO_2}  ({ m Torr})^{\rm a}$
	Theory <sup>b</sup>	Experiment	Corrected	Theory	Experiment	Theory	Experiment	Theory	Experiment	
Ag <sub>2</sub> CO <sub>3</sub>	371	420 [34]	387	$4 \times 10^{-5}$		102	96 [34]	143		
CdCO <sub>3</sub>	442	513 [35]	469	$2 \times 10^{-3}$		135	151 [35]	270	272 [35] 268 [36]	1.5 50–200
ZnCO <sub>3</sub>	497	523 [37]	508	$4 \times 10^{-8}$		151	159 [37], 161 [38]	302	251 [39] 280 [39]	10 100
MgCO3	689	714 [40]	705	$8  imes 10^{-9}$		204	192 [40], 150 [41]	408	450 [42]	760
CaMg(CO <sub>3</sub> ) <sub>2</sub>	809	824 [6]	820	$5  imes 10^{-6}$	$1 \times 10^{-4}$ [6]	234	195 [6], 221 [43]	468		
CaCO <sub>3</sub>	895	934 [11]	928	$5 \times 10^{-5}$	$2 \times 10^{-5}$ [11,44]	253	220 [11], 209 [11] 205 [44], 222 [45]	506		
SrCO <sub>3</sub>	908	888 [46]	887	$5  imes 10^{-3}$		261	290 [46], 222 [47]	522		
BaCO <sub>3</sub>	1205 <sup>c</sup>	1215 [47]	1214	$2 \times 10^{-4}$	$2 \times 10^{-4}$ [7]	319 <sup>c</sup>	283 [47], 264 [48] 226 [7]	639 <sup>c</sup>	643 [48]	3.5

Table 1 Kinetic parameters for thermal decomposition of carbonates

<sup>a</sup> 1 Torr = 133.322 Pa.

<sup>b</sup> At  $P_{\rm CO_2} = 3 \times 10^{-7}$  bar.

<sup>c</sup> At  $\tau = 0$ .

### 3.2. Experimental kinetic data

Despite a wealth of publications in this field, the possibilities of choosing reliable experimental data which would characterize the decomposition kinetics of carbonates are fairly limited. Preference was given to a series of studies under isothermal conditions performed in the mid-1970s by Searcy and colleagues, devoted to the decomposition of CaCO<sub>3</sub> [6,11],  $CaMg(CO_3)_2$  [6] and  $BaCO_3$  [7], as well as to the publications of Pavlyuchenko [37], who studied decomposition of CdCO<sub>3</sub> [35], ZnCO<sub>3</sub>, MgCO<sub>3</sub> [40] and SrCO<sub>3</sub> [46]. In case of Ag<sub>2</sub>CO<sub>3</sub>, we used the only available data from a publication by Spencer and Topley in 1929 [34]. Some data were taken from the works by Hüttig et al. [38] (ZnCO<sub>3</sub>), Britton et al. (MgCO<sub>3</sub> [41] and CaMg(CO<sub>3</sub>)<sub>2</sub> [43]), Judd and Pope [47] (SrCO<sub>3</sub> and BaCO<sub>3</sub>) and from a recent publication by Maciejewski [45] (CaCO<sub>3</sub>).

In all these works (except [45]), measurements were carried out under continuous pumping of the furnace to  $10^{-7}$ – $10^{-8}$  bar (the equimolar mode). For CdCO<sub>3</sub>, ZnCO<sub>3</sub>, MgCO<sub>3</sub> and BaCO<sub>3</sub>, the experimental values of *E* parameter in the presence of CO<sub>2</sub> (the isobaric mode) were also included. Samples of natural crystals of known size were used in the experiments of Searcy and his colleagues and powders, in the experiments of all other workers. The mass change were measured continuously with a quartz microbalance [34–48] or

by the torsion–Langmuir technique [6,7]. The manometric technique with an ion-gauge was used only in [11]. When runs to be made in  $CO_2$ , the diffusion pump was turned off and  $CO_2$  was held at a steadystate level by adjusting a leak value.

### 3.3. Theoretical kinetic data

Theoretical values of E and  $T_{in}$  parameters in Table 1 were calculated with the use of thermodynamic functions tabulated in [49,50]. Table 2 presents the values of enthalpy and entropy changes for the deduced decomposition reactions. Eqs. (11) and (12) were used for the calculation of  $E^{e}$  and  $E^{i}$  parameters and Eq. (17) was used for the calculation of  $T_{in}$  parameter. In the calculations of the enthalpy of decomposition reactions for all the carbonates except of BaCO<sub>3</sub>, we took into account the transfer of one-half of the condensation energy to the reactant ( $\tau = 0.5$ ). For BaCO<sub>3</sub>, the best correlation between experiment and theory corresponds to the condition  $\tau = 0$ . This means that, for reasons unknown to us, any energy transfer to the reactant in the process of condensation of low-volatility molecules of BaO is absent. The values of  $\Delta S_{\rm T}^{\rm o}/v$ (see the last column in Table 2) are in agreement with the regularity  $\Delta S_{\rm T}^{\rm o}/v = 150 \pm 30 \, {\rm J} \, {\rm mol}^{-1} \, {\rm K}^{-1}$ (Section 2.4) valid for different classes of solids.

In the calculations of the initial temperatures of decomposition, we assumed that this temperature

Reaction <sup>a</sup>	v	τ	$\Delta H_{ m T}^{ m o}$	$\Delta S_{\mathrm{T}}^{\mathrm{o}}$	$\Delta S_{\mathrm{T}}^{\mathrm{o}}/v$
			$(kJ mol^{-1})$	$(\operatorname{J}\operatorname{mol}^{-1}\operatorname{K}^{-1})$	$(\operatorname{J}\operatorname{mol}^{-1}\operatorname{K}^{-1})$
$\overline{\mathrm{Ag}_2\mathrm{CO}_3 \to 2\mathrm{Ag}(\mathrm{g})\downarrow + 0.5\mathrm{O}_2 + \mathrm{CO}_2}$	3.5	0.5	358.0 <sub>298</sub>	494.6298	141.3
$CdCO_3 \rightarrow CdO(g) \downarrow + CO_2$	2	0.5	270.1 <sub>298</sub>	356.2 <sub>298</sub>	178.1
$ZnCO_3 \rightarrow ZnO(g) \downarrow + CO_2$	2	0.5	302.1 <sub>298</sub>	355.9 <sub>298</sub>	178.0
$MgCO_3 \rightarrow MgO(g) \downarrow + CO_2$	2	0.5	408.5900	343.1900	171.6
$0.5$ CaMg(CO <sub>3</sub> ) <sub>2</sub> $\rightarrow 0.5$ CaO(g) $\downarrow + 0.5$ MgO(g) $\downarrow + CO_2$	2	0.5	$468.2_{900}$	328.9 <sub>900</sub>	164.5
$CaCO_3 \rightarrow CaO(g) \downarrow + CO_2$	2	0.5	505.9900	314.6900	157.3
$SrCO_3 \rightarrow SrO(g) \downarrow + CO_2$	2	0.5	$522.2_{900}$	322.1 <sub>900</sub>	161.1
$BaCO_3 \rightarrow BaO(g) + CO_2$	2	0	638.7 <sub>1200</sub>	275.21200	137.6

Table 2 Enthalpy and entropy changes for the deduced decomposition reactions of carbonates [49,50]

<sup>a</sup> An arrow ( $\downarrow$ ) implies taking into account the condensation energy transfer to the reactant.

corresponds to the initial pressure of evolved CO<sub>2</sub>,  $P_{\rm in} = 3 \times 10^{-7}$  bar. In our estimates, this magnitude is close within a factor of 3 to the true values of  $P_{\rm in}$  in different works. Because of different techniques, instrumentation and experimental conditions used in different studies, this parameter is subject to variation in the range from  $10^{-7}$  to  $10^{-6}$  bar.

# 3.4. Correlation between experimental and theoretical values of $T_{in}$

Most studies of the decompositions of powders and single crystals in thermal analysis tacitly assume that the temperature of the sample is equal to that of the furnace, and that the self-cooling due to some heat being expended in the endothermic decomposition can be neglected. However, as early as 1931, Smith and Topley [51] showed that the temperature of a single crystal in vacuum was lower than that in the furnace by 4–8 K. It is rather obvious that, for powders, the selfcooling effect should be much greater.

L'vov et al. [20,52] proposed a fairly simple theoretical model and developed a program to compute the temperature of individual crystals and the layer-bylayer temperature distribution in powder samples during the course of their decomposition in vacuum and in the presence of foreign gases. Simulation of the temperature distribution, inside a powder sample, can be reduced to modelling the vertical distribution between horizontal layers of this material of thickness equal to the powder grain diameter. If the furnace temperature is the same on top and at the bottom of the sample, the analysis can be limited to considering only one-half of such multilayered sample, from the central, 0th or 1st layer, to the *n*th outermost layer. All the calculations were performed with the laboratory-developed computer program described in [52].

As an illustration of the value of self-cooling effect for the decomposition of single crystals of carbonates in vacuum  $(10^{-7} \text{ bar})$ , Fig. 1 presents the results of calculations of the temperature of the sample (reactant),  $T_{\rm s}$ , related to the temperature of the furnace,  $T_{\rm f}$ . It can be seen that the  $T_s/T_f$  ratio depends not only on the absolute rate of decomposition (or the partial pressure of evolved CO<sub>2</sub>). The effect is increased with reducing of the decomposition temperature. For example, the  $P_{\rm CO_2}$  values, corresponding to  $T_{\rm s}/T_{\rm f} = 0.95$ , equal to about  $3 \times 10^{-4}$  bar for BaCO<sub>3</sub>,  $5 \times 10^{-5}$  bar for CaCO<sub>3</sub> and  $5 \times 10^{-6}$  bar for CdCO<sub>3</sub>. It is easy to understand. Heating of the sample via the radiation from the furnace (in accord with the Stefan-Boltzman Law), is dramatically reduced with a temperature decrease.

The corrected  $T_{in}$  values given in Table 1 were calculated in the same manner. They correspond to the true temperatures of single crystals of carbonate in the process of their decomposition in furnaces at the initial temperatures of experiments. It should be mentioned that the emittance parameter  $\varepsilon$  in the calculations was assumed to be equal to its maximum value ( $\varepsilon = 1$ ) and therefore the corrected values of temperature correspond to their maximum allowable values. As can be expected, the effect of self-cooling is more pronounced at low temperatures. The  $T_s/T_f$  ratio is about 0.92 for Ag and Cd carbonates, 0.95 for ZnCO<sub>3</sub> and higher than 0.994 for CaMg, Ca, Sr and Ba carbonates.

The correlation between theoretical and experimental (corrected) values of the initial decomposition



Fig. 1. The self-cooling effect for the decomposition of CdCO<sub>3</sub>, CaCO<sub>3</sub> and BaCO<sub>3</sub> in vacuum.

temperatures is presented in Fig. 2. The agreement is excellent though, we should admit, is rather accidental, if we take into account the discrepancies between initial temperatures listed for the same carbonate (e.g. CaCO<sub>3</sub>) by different authors. As can be seen from the correlation equation (see Fig. 2), a mean systematic overestimation of experimental (corrected) values over theoretical values is about 25 K.



Fig. 2. Correlation of theoretical and experimental (corrected) values of the initial temperatures of decompositions presented in Table 1.

For CaMg(CO<sub>3</sub>)<sub>2</sub>, CaCO<sub>3</sub> and BaCO<sub>3</sub>, the values of  $\alpha_v$  were included in Table 1. They correspond to the ratio of decomposition rates (or, what is the same, to the ratio of equivalent pressures of CO<sub>2</sub>) for the equilibrium and deduced schemes of decompositions. Experimental values of  $\alpha_v$  were measured by the torsion–effusion and torsion–Langmuir methods. The agreement for CaCO<sub>3</sub> and BaCO<sub>3</sub> is excellent. Twenty times difference between theory and experiment in  $\alpha_v$  for CaMg(CO<sub>3</sub>)<sub>2</sub> may be attributed to the underestimation of the decomposition rate in case of effusion experiments [6].

# 3.5. The self-cooling effect and measurements of *E* parameters

Effect of self-cooling on measured values of the E parameter is much more pronounced than that on the  $T_{\rm in}$  parameter. This results from higher mean temperature used for the determination of E parameter. (The initial temperature usually corresponds to the lowest value of the temperature interval). The method of corrections of kinetic parameters and particularly of the *E* parameter for the self-cooling effect was described earlier [20]. To remind, it consists in the following. The deviation of the measured E parameter from the true value, which corresponds to the assumed spatially uniform sample heating up to the furnace temperature, is determined, first, by the difference between the temperatures of the furnace,  $T_{\rm f}$ , and of the sample surface,  $T_s$ , and second, by the effective number of powdered layers  $n_{\rm e}$  involved in decomposition. The last factor corresponds to the effective number of powdered sample layers whose decomposition occurs at the same rate as that of the surface layer. Taking into account these two factors, the

Table 3 Correction of measured values of E parameters for the self-cooling effect

corrected value of the E parameter can be calculated using the relationship [20]

$$E_{\rm cor} = \frac{(1/T_{\rm f}' - 1/T_{\rm f}'')E_{\rm exp} + R\ln(n_{\rm e}'/n_{\rm e}'')}{1/T_{\rm s}' - 1/T_{\rm s}''}$$
(18)

Here one and two primes refer, respectively, to the lower and higher temperatures used to determine E and the corresponding parameters  $n_e$ , and the subscript 'exp', to the experimental value of the E parameter.

Eq. (18) can be applied not only to powders but also to single crystals. In this case,  $n_e = 1$ , and the calculation of corrections takes into account only the temperatures of the furnace and of the sample. In case of powders, for the calculation of  $n_e$  factors it is necessary to know the actual number of layers n in the sample. For spherical particles, this can be calculated using the relationship [20]

$$n = \frac{12}{\pi^2} \frac{m}{\rho r_0 d^2} \tag{19}$$

Here m,  $\rho$ ,  $r_0$  and d are, respectively, the mass and density of the reactant, the grain radius and the diameter of the balance pan on which the sample is placed.

The described method was used in this study for the evaluation of the self-cooling effect on the *E* parameters in the experiments of Searcy et al. with CaCO<sub>3</sub> [44], CaMg(CO<sub>3</sub>)<sub>2</sub> [6] and BaCO<sub>3</sub> [7] and in the experiments with CaCO<sub>3</sub> (in vacuum and nitrogen) described recently by Maciejewski [45]. Table 3 presents the results of this evaluation. Single crystals were used in the experiments of Searcy et al. [6,7,44] and powders in [45]. For the calculation of total number of layers, *n*, in powdered samples of CaCO<sub>3</sub>, we used the following magnitudes of parameters [53]: m = 20 mg =  $2 \times 10^{-5}$  kg,  $\rho = 2710$  kg m<sup>-3</sup>,  $r_0 = 7.5$  µm =

Carbonate	$T_{\min}$ (K)		$T_{\max}$ (K)		$P_{\rm air}$ (bar)	n	n <sub>e</sub>		$E (\text{kJ mol}^{-1})$		Reference
	Measured	Corrected	Measured	Corrected			$T_{\min}$	$T_{\rm max}$	Measured	Corrected	
CaCO <sub>3</sub>	934	928.38	1013	984.43	$1 \times 10^{-7}$	1	1	1	205	278.8	[44]
CaCO <sub>3</sub>	788	787.68	823	821.82	$5  imes 10^{-4}$	15	13.12	9.72	222	274.5	[45]
CaCO <sub>3</sub>	973	972.03	1046	1040.87	1	15	11.52	5.64	180	277.2	[45]
$CaMg(CO_3)_2$	824	819.94	900	873.93	$1 \times 10^{-7}$	1	1	1	191.6 <sup>a</sup>	260.6	[6]
BaCO <sub>3</sub>	1160	1159.83	1210	1209.44	$1 \times 10^{-7}$	1	1	1	225.9	227.5	[7]

<sup>a</sup> Recalculated on the basis of tabulated data reported in [6].

 $7.5 \times 10^{-6}$  m and d = 6.3 mm  $= 6.3 \times 10^{-3}$  m. The calculations were performed with a computer program described in [52].

As can be seen from the results in Table 3, in all cases of CaCO<sub>3</sub> decompositions, the corrected values of *E* are close to 277 kJ mol<sup>-1</sup>. This is 9% higher than the theoretical value ( $253 \text{ kJ mol}^{-1}$ ). However, this discrepancy is 2-3 times smaller than that between the theoretical and original data. Moreover, irrespective of the differences in experimental conditions, the corrected values practically coincide. It is interesting that in case of powders (in vacuum and nitrogen), the difference between the temperatures of the furnace and samples is very small (<0.5% even for the maximum temperatures), so that the final large differences in the *E* parameters are mainly due to the difference in  $n_{\rm e}$  factors for different (minimum and maximum) temperatures. In case of  $CaMg(CO_3)_2$ , the corrected value of E (260.6 kJ mol<sup>-1</sup>) is also about 10% higher than the theoretical value  $(234 \text{ kJ mol}^{-1})$ . This is nearly 2 times smaller than the discrepancy with the original value  $(191.6 \text{ kJ mol}^{-1})$ . Only in case of BaCO<sub>3</sub> the correction value is small  $(1.6 \text{ kJ mol}^{-1})$ .

This is in accord with the results of calculations presented in Fig. 1.

# 3.6. Correlation between experimental (uncorrected) and theoretical values of *E*

Fig. 3 presents the correlation between theoretical and available experimental values of the E parameters for both the equimolar and isobaric modes of decomposition for eight carbonates under investigation (Table 1). As can be seen from the correlation equation (see Fig. 3), the general agreement is quite satisfactory (a mean systematic underestimation of experimental values the *E* parameter is only about  $19 \text{ kJ mol}^{-1}$ ), though the scatter of experimental results from a correlation line is rather high. The mean relative value of the standard deviation is about 11%. This is 4 times larger than that for the  $T_{in}$  parameter. Despite this at first sight satisfactory agreement, there are some doubts in the correctness of some experimental results, especially those which are greater than the theoretical values. These doubts are connected with the expectation of the serious decreasing effect of self-cooling on



Fig. 3. Correlation of theoretical and experimental values of the *E* parameters presented in Table 1.

the *E* values obtained in high vacuum for powder samples (CdCO<sub>3</sub>, ZnCO<sub>3</sub>, MgCO<sub>3</sub> and SrCO<sub>3</sub>). Contrary to these expectations, the values of the *E* parameter for these carbonates in some cases are equal to (or even greater than) the theoretical values. As a result, they partly 'equilibrate' the underestimated values of the *E* parameter for other carbonates and produce the apparent agreement between theory and experiment.

The most plausible reason of overestimation of the *E* parameters in the experiments with Cd, Zn, Mg and Sr carbonates performed by Pavlyuchenko and his colleagues [35,37,39,40,46] is, in our opinion, in an appropriate mathematical model used for processing of primary experimental data ( $\alpha$ , *t*). They used the very popular Avrami–Erofeev model with the variable *n* factor derived for sigmoid  $\alpha$ -time curves (see, e.g. [2]). This model takes into account nucleation and growth processes which are typical for most of carbonates. However, these stages of decomposition do not give true information about the *steady-state rate* of decomposition at the deceleratory stage, which an accord with the physical approach [23] is

the only parameter suitable for the strict quantitative interpretation. We can assume that the overestimation of the *E* parameters is the result of application of the Avrami-Erofeev model. To prove this supposition, we have investigated several publications by Pavlyuchenko and his colleagues, and in one of them [54], we have found a comparison of the results obtained from processing of the same data (for the decomposition of CdCO<sub>3</sub>) with the Avrami-Erofeev (An) and contracting volume (R3) models. These data are presented in Fig. 4. It can be seen that a slope of the Arrhenius graph for An model is 1.34 times higher that that for the R3 model. We are conscious that this particular fact is not enough for general conclusions, and this problem needs further consideration. Nevertheless, in support of this conjecture one can refer to the results reported for the recent ICTAC kinetics project [45,55]. The discrepancy between E parameters obtained by different workers from kinetic analysis of identical sets of data (in particular, for CaCO<sub>3</sub> decomposition), using different computational procedures, was much worse than might have been be expected.



Fig. 4. The Arrhenius graphs for the decomposition of CdCO<sub>3</sub> corresponding to the different mathematical models used in [54] for processing of the same set of primary data.

#### 3.7. Validation criteria for measured E parameters

Of two kinetic parameters (A and E) entering the Arrhenius equation, only the E parameter is usually used for the interpretation of the mechanisms of decompositions. This explains why in a majority of publications, authors report only E values. Variations of the A parameter in very wide limits and, in particular, observing of high values of A in the presence of gaseous products have not found any theoretical explanation in the framework of the traditional ideas. This problem has been solved in the framework of the physical approach to the interpretation of decomposition kinetics. As it was shown above (see Section 2.3), the isobaric mode of decomposition results in much higher values of A compared to that for the equimolar mode.

However, in the absence of gaseous products in the reactor (e.g. in vacuum), the values of A parameter can vary only within narrow limits. It is clear from the analysis of Eq. (13). Let us estimate its average value and the limits of variation in case of the decomposition of carbonates. If we take into account that the radius of a spherical particle for a sample taken as a single crystal or powder can vary from 0.01 to 1 mm, then with a factor of 10 the average radius  $r_0 = 1 \times 10^{-4}$  m. The average value of  $\Delta S_{\rm T}^{\rm o}/v$  for the carbonate decomposition is  $160 \pm 20 \text{ J mol}^{-1} \text{ K}^{-1}$  (see Table 2). The variations (for different carbonates) of other parameters entering Eq. (13) are smaller. We can use for this purpose the averaged magnitudes:  $\rho = 3000 \text{ kg m}^{-3}$ ,  $M_r = 0.1 \text{ kg mol}^{-1}, \overline{M} = 0.05 \text{ kg mol}^{-1} \text{ and } T = 700 \text{ K}.$ It follows from these results that the  $\ln(A)$  (s<sup>-1</sup>) parameter can vary from 21 to 31 (taking into account the maximum variations of the entropy of reaction and particle size).

From the above reasoning it is clear that any deviation of the  $\Delta S_{\rm T}^{\rm o}/\nu$  or ln(*A*) (s<sup>-1</sup>) parameters from the limits defined should be interpreted as a defect (or

defects) in the experimental or computational stages of kinetic analysis and a warning of a possible error in the determination of the E parameter. At the same time, the agreement of the reaction entropy or Aparameter with the limits defined should be considered only as the *necessary*, *but not the sufficient* condition for the correctness of measured E value. This is connected with a possibility of interference of two or more effects (opposite in sign) which can partly or completely compensate each other.

Besides these two interrelated criteria, there is one more criterion of the validity based on the ratio of the initial temperature of decomposition to the *E* parameter,  $T_{in}/E$ . As shown above (Section 2.4), this ratio is rather constant for different solids. In case of carbonates, when  $140 < \Delta S_T^o/\nu < 180$  (in J mol<sup>-1</sup> K<sup>-1</sup>) and  $10^{-7} < P_{in} < 10^{-6}$  (in bar), we obtain from Eq. (17):  $3.2 < T_{in}/E < 3.9$  (in K mol kJ<sup>-1</sup>).

To illustrate the efficiency of these criteria, we have applied them to some of the data discussed above. Tables 4–6 present the results of such consideration with the use each of the parameters mentioned above. For MgCO<sub>3</sub> and SrCO<sub>3</sub>,  $\ln(A)$  (s<sup>-1</sup>) and  $T_{in}/E$  parameters were used, for other carbonates,  $\Delta S_T^o/\nu$  and  $T_{in}/E$ parameters. From examination of these results, the following conclusions can be deduced:

- 1. The *E* parameter for SrCO<sub>3</sub> reported in [46] is slightly overestimated. This is supported by the higher value of  $\ln(A)$  (s<sup>-1</sup>) parameter and lower value of  $T_{in}/E$  ratio (compared with their theoretical values).
- 2. The *E* parameter for MgCO<sub>3</sub> reported in [40] is slightly underestimated, and this is in accord with the smaller value of  $\ln(A)$  (s<sup>-1</sup>) parameter and higher value of  $T_{in}/E$  ratio (compared with their theoretical values).
- 3. The *E* parameters for  $CaMg(CO_3)_2$ ,  $CaCO_3$  and  $BaCO_3$  reported in [6,7,44] are strongly underestimated, and this is in accord with the much

Table 4

Experimental and theoretical values of ln(A) (s<sup>-1</sup>) for the decomposition of Sr and Mg carbonates

Carbonate	$\ln(A) \ (s^{-1})$		$\Delta \ln(A) (s^{-1})$	$E (\mathrm{kJ}\mathrm{mol}^{-1})$	$\Delta E (\mathrm{kJ}\mathrm{mol}^{-1})$	
	Experiment	Theory		Experiment	Theory	
SrCO <sub>3</sub>	26.1 [46]	25.9	0.2	290 [46]	261	29
MgCO <sub>3</sub>	20.3 [40]	27.2	-6.9	192 [40]	204	-12

Carbonate	$\Delta S_{\rm T}^{\rm o}/\nu  ({\rm J}{ m mol}^{-1}{ m K}$		$\frac{\Delta(\Delta S_{\rm T}^{\rm o}/\nu)}{(\rm Jmol^{-1}K^{-1})}$	$E (\text{kJ mol}^{-1})$	$\Delta E \; (\text{kJ mol}^{-1})$					
	Experiment	Theory		Experiment	Theory					
CaMg(CO <sub>3</sub> ) <sub>2</sub>	93±6 [6]	164	-71	195 ± 1 [6]	234	-39				
CaCO <sub>3</sub>	84 ± 12 [11]	157	-73	$209 \pm 12$ [11]	253	-44				
BaCO <sub>3</sub>	54 ± 3 [7]	138	-84	$226 \pm 7$ [7]	319	-93				

Table 5 Experimental and theoretical values of entropy for the decomposition of alkaline-earth carbonates (in order of decreasing experimental values of  $\Delta S_{\alpha}^{o}/\nu$ )

Table 6

Experimental and theoretical values of  $T_{in}/E$  ratio for the decomposition of alkaline-earth carbonates (in order of increasing  $T_{in}/E$  ratio)

Carbonate	$T_{\rm in}~({\rm K})$	$E (\text{kJ mol}^{-1})$	Reference	$T_{\rm in}/E$ (K mol kJ <sup>-1</sup> )		Experiment to	$E (\text{kJ mol}^{-1})$		$\Delta E \; (\text{kJ mol}^{-1})$
				Experiment	Theory	theory ratio	Experiment	Theory	
SrCO <sub>3</sub>	888	290	[46]	3.1	3.5	0.89	290	261	29
MgCO <sub>3</sub>	714	192	[40]	3.7	3.4	1.09	192	204	-12
$CaMg(CO_3)_2$	824	195	[6]	4.2	3.5	1.20	$195 \pm 1$	234	-39
CaCO <sub>3</sub>	934	209	[11]	4.5	3.4	1.32	$209 \pm 12$	253	-44
BaCO <sub>3</sub>	1163	226	[7]	5.1	3.8	1.34	$226\pm7$	319	-93

smaller values of  $\Delta S_{\rm T}^{\rm o}/\nu$  parameter and higher values of  $T_{\rm in}/E$  ratio (compared with their theoretical values).

The use of these criteria allows to exclude from succeeding consideration the wrong data. For example, for the isothermal decomposition of CaCO<sub>3</sub> in vacuum, a set of E and  $\ln(A)$  (s<sup>-1</sup>) parameters calculated by different workers were reported (Table 3, [55]). From a list of  $\ln(A)$  (s<sup>-1</sup>) values (24.78; 25.96; 32.10; 24.91; 32.10; 25.94; 21.3; 36.25; 11.04; 25.66; 13.43; 25.13 and 3.68), more than half of them (32.10; 32.10; 21.3; 36.25; 11.04; 13.43 and 3.68) can be rejected as erroneous because they are outside the limits for variation of this parameter (23-28) in case of CaCO<sub>3</sub>. This does not mean that all other data in this list are correct because of the possibility of interference of two or more effects (opposite in sign) which can compensate each other. As examples of such effects, the self-cooling effect, on the one hand, and the inappropriate kinetic model used for the calculations, on the other, may be mentioned. It is worth to note that the same conclusion about the validity of the above set of data can be made, if we compare experimental and theoretical values of the  $T_{\rm in}/E$  ratio.

# 3.8. The Topley–Smith (T-S) effect for the decomposition of $CaCO_3$

Anomalous variation of the rate of dehydration of crystalline hydrates with increasing water vapor pressure  $(P_w)$  was discovered by Topley and Smith 70 years ago [56] in a study of the rate of dehydration of  $MnC_2O_4 \cdot 2H_2O$ . In contrast to the expected monotone decrease of the rate with increasing  $P_{\rm w}$ , the dehydration rate, on reaching a certain critical pressure  $(10^{-5} 10^{-4}$  bar), begins to grow, passes through a maximum, and falls off again. In the time elapsed thereafter, the T-S effect was observed in a score of different crystalline hydrates [52]. A recent theoretical study [52] has shown that this anomaly is actually the result of competition between the depressing influence of water vapor during dehydration, on the one hand, and the increasing heat transfer from the furnace to the sample by water vapor, on the other, in the presence of intense self-cooling. The computer model developed [52] accounted for all the main features of the T-S effect, in particular, the enhancement of the effect with increasing decomposition temperature and with decreasing powder grain size. The main argument against this interpretation is the fact that the T-S effect has been observed up to now only for the



Fig. 5. Effect of  $CO_2$  pressure on the rate of decomposition of CaCO<sub>3</sub>. Two sets of the experimental data (points) are taken from [11]. Theoretical curves were calculated for the different emittance factors: 0.020 (above) and 0.015 (below).

decompositions of crystalline hydrates and, therefore, this effect (as might appear) should be connected with some particular features of dehydration reactions.

To prove that T-S effect can be observed in case of other decomposition reactions, we simulated  $J = f(P_{CO_2})$  curve for the decomposition of a single crystal of CaCO<sub>3</sub> at 1000 K in the presence of  $10^{-6}$ - $10^{-3}$  bar CO<sub>2</sub>. The same computer program was used as before [52]. It was assumed that the heat expended for the decomposition is compensated by the radiation emitted from the heater and through heat transfer by the gas molecules of  $CO_2$ . It was found that under these conditions the T-S effect can be observed if the emittance factor,  $\varepsilon$ , is smaller than 0.02 (Fig. 5). At higher values of  $\varepsilon$ , a maximum disappears, and only a small bend of the curve can be observed. In this case, the effect of self-cooling is smaller and therefore the increase of temperature of CaCO3 with CO2 pressure is compensated by the retardation effect of CO<sub>2</sub> on the decomposition (in the isobaric mode).

It happened that the effect of  $10^{-6}$ – $10^{-3}$  bar CO<sub>2</sub> on the decomposition of CaCO<sub>3</sub> at different temperatures (898, 983, 1006 and 1073 K) has been investigated by Darroudl and Searcy [11]. The vacuum chamber with

internal hairpin-shaped heating elements connected in parallel was used. To reduce temperature gradients and contamination of the samples by condensable products of reaction of  $CO_2$  with the tungsten filaments, a platinum cylinder 3 cm in diameter and 10 cm long was placed around the sample. It means that heating of the sample by radiation from the tungsten filament has been performed through the intermediate heating of Pt cylinder. Moreover, the emittance of platinum is rather low. At 1000 K, ε is about 0.10 [57] or 0.08 [58]. We can conclude that as a result of these two factors, the actual magnitude of  $\varepsilon$  in these experiments was smaller than 0.08. Be it as it may, in some of the figures (at 983, 1006 and 1073 K) in this work, we can clearly observe the effect of bending of, and even the appearance of a maximum on,  $J = f(P_{CO_2})$  curves. As an illustration, we reproduce in Fig. 5 the experimental data obtained at 1006 K. The shape of theoretical and experimental curves is very similar. As expected from our calculations, the maximum (or bending) is observed at about  $10^{-4}$  bar. Moreover, the absolute rates of decompositions differ from theoretical ones not more than by a factor of 2. The agreement is excellent if we take into account the simplifications of the calculation model and experimental errors.

The other important conclusion, which can be deduced from examination of these experimental results [11], is connected with the discrepancy in the dependence of decomposition rates of CaCO<sub>3</sub> on CO<sub>2</sub> background pressures observed by different authors (hyperbolic rate law in [8-10] and close to linear decrease observed by Darroudl and Searcy [11]). This is also connected with the effect of severe self-cooling of samples in high vacuum. Instead of expected two orders decrease of the decomposition rate in the range from  $10^{-6}$  to  $10^{-4}$  bar CO<sub>2</sub>, its value retained practically constant. This is in accord with our direct calculations of self-cooling effect (Section 3.4). Only at CO<sub>2</sub> pressure higher than  $10^{-4}$  bar used in [8-10], the self-cooling effect is significantly reduced and the dependence of decomposition rates approximates to the hyperbolic law.

### 4. Conclusions

The following conclusions can be made on the basis of this study:

- 1. The effect of self-cooling of reactant is of primary importance in the explanation of many controversial results obtained by different researchers in investigations of the kinetics of carbonate decomposition. In all cases of decompositions in vacuum, it is responsible for the experimental underestimation of the E parameters and overestimation (at temperatures lower than ca. 500 K) of the initial temperatures of decomposition,  $T_{in}$ . This effect cannot be avoided for the decomposition of powdered samples at any conditions (even in an atmosphere of foreign gases) because of the serious temperature gradient inwards different at different temperatures. Probably, experiments with single crystals of carbonates in an atmosphere of  $CO_2$  (10<sup>-3</sup>-10<sup>-2</sup> bar) might correspond to the best approximation to the spatially isothermal heating conditions. In the last case, due to the additional heat transfer by CO<sub>2</sub> and higher temperature of decomposition in the isobaric mode, the effect of self-cooling is smaller. For example, at 1000 K and  $\varepsilon = 1$ , the temperature of a single crystal of CaCO<sub>3</sub> in the presence of  $10^{-2}$  bar of CO<sub>2</sub> should be about 999.98 K instead of 977 K in vacuum.
- 2. In this context, the data on the *E* parameter obtained by Searcy et al. [6,7,11,44] for the decomposition of CaCO<sub>3</sub>, CaMg(CO<sub>3</sub>)<sub>2</sub> and BaCO<sub>3</sub> in high vacuum, which are considered as a standard of accuracy and a sort of reference values in carbonate decompositions, are also erroneous. The belief expressed by Beruto and Searcy in [44] ('The design of the apparatus used in the present study reduces the heat transfer problem to a negligible source of error in the temperature and decomposition pressure range used') was too optimistic.
- 3. The self-cooling effect in the decomposition of CaCO<sub>3</sub> in the presence of CO<sub>2</sub>  $(10^{-6}-10^{-4} \text{ bar})$  is responsible for the lack of expected hyperbolic dependence of decomposition rate on CO<sub>2</sub> pressure and the appearance of the T–S effect [11].
- 4. The effect of overestimation of the *E* parameters reported by Pavlyuchenko et al. [35,37,39,40,46] for Cd, Zn, Mg and Sr carbonates has been revealed. It is most likely connected with an inappropriate mathematical model (An) used for processing of primary experimental data ( $\alpha$ , *t*).

- 5. Several criteria, which should be considered as the necessary, but not the sufficient condition for the validity of measured *E* values, have been proposed. These include the fulfilment of the conditions:  $140 < \Delta S_{\rm T}^{\rm o}/\nu < 180$  (in J mol<sup>-1</sup> K<sup>-1</sup>) or  $21 < \ln(A)$  (s<sup>-1</sup>) < 31 or  $3.2 < T_{\rm in}/E < 3.9$  (in K mol kJ<sup>-1</sup>).
- 6. The results of examination of the available literature data (the *E* and  $T_{in}$  parameters) for decomposition of carbonates and their comparison with the theoretical calculations in the framework of the physical approach support the general mechanism of decomposition which includes as a primary stage the congruent dissociative evaporation of reactants. For all the carbonates, except of BaCO<sub>3</sub>, the transfer to the reactant one-half of the energy released in the course of the condensation of low-volatility product has been taken into account. The reason of the exception of BaCO<sub>3</sub> from this rule requires further investigation.

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